# INDIAN SCHOOL MUSCAT <br> FINAL TERM EXAMINATION <br> MATHEMATICS 

CLASS: X
18.11.2018

Sub.Code: 041

## General Instructions:

1. All the questions are compulsory.
2. The questions paper consists of $\mathbf{3 0}$ questions divided into 4 sections $\mathrm{A}, \mathrm{B}, \mathrm{C}$ and D.
3. Section A comprises of $\mathbf{6}$ questions of $\mathbf{1}$ mark each. Section B comprises of $\mathbf{6}$ questions of $\mathbf{2}$ marks each.

Section C comprises of $\mathbf{1 0}$ questions of $\mathbf{3}$ marks each. Section $\mathbf{D}$ comprises of $\mathbf{8}$ questions of $\mathbf{4}$ marks each.
4. There is no overall choice. However, an internal choice has been provided in two questions of 1 mark each, two questions of 2 marks each, four questions of 3 marks each and three questions of 4 marks each. You have to attempt only one of the alternatives in all such questions.
5. Use of calculators is not permitted.

## SECTION - A <br> (Questions 1 to 6 carry 1 mark each)

1. Find the value of $a$, if the distance between the points $A(-3,-14)$ and $B(a,-5)$ is 9 units

## (OR)

$\mathrm{A}(5,1), \mathrm{B}(1,5)$ and $\mathrm{C}(-3,-1)$ are the vertices of $\triangle \mathrm{ABC}$. Find the length of median AD .
2. Write a quadratic polynomial, the product and sum of whose zeroes are $\frac{-9}{2}$ and $\frac{-3}{2}$ respectively.
3. After how many decimal places will the decimal expansion of $\frac{26}{2^{4} \times 5^{3}}$ terminate?
4. If $\sin \theta=\frac{1}{3}$, thenfindthevalueof $\left(2 \cot ^{2} \theta+2\right)$.
(OR)
$\triangle A B C$ is right angled at C , if $\tan \mathrm{A}=\frac{1}{\sqrt{3}}$, find $\cos \mathrm{B}$.
5. Find the length of tangent drawn to a circle with radius 8 cm from a point 17 cm away from the centre of the circle.
6. Find the mode of the data, using an empirical formula, when it is given that median $=41.25$ and mean $=$ 33.75 .

## SECTION - B

## (Questions 7 to 12 carry 2 marks each)

7. If $\sec \mathrm{A}=\frac{2}{\sqrt{3}}$, find the value of $\frac{1+\sin A}{\tan A}$
8. A card is drawn at random from a well shuffled deck of 52 cards. Find the probability of getting neither a red card nor a queen.
9. The ratio of the height of a tower and the length of its shadow on the ground is $\sqrt{3}: 1$. What is the angle of elevation of the sun?
10. Draw a circle of radius 3 cm . From a point $P, 6 \mathrm{~cm}$ away from its centre, construct a pair of tangents to the circle.

## (OR)

Draw a line segment AB of length 7 cm . Using ruler and compasses, find a point P on AB such that $\frac{A P}{A B}=\frac{3}{5}$
11. If $\tan (3 x+30)^{\circ}=1$, then find $x$.

## (OR)

If in $\triangle \mathrm{ABC}, \angle \mathrm{A}=90^{\circ}$ then find the value of $\cos ^{2} \mathrm{~B}+\cos ^{2} \mathrm{C}$
12. For the following cumulative frequency distribution, find the modal class.

| Marks | Below 10 | Below 20 | Below 30 | Below 40 | Below 50 | Below 60 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 3 | 12 | 27 | 57 | 75 | 80 |

SECTION - C
(Questions 13 to 22 carry 3 marks each)
13. Use Euclid's Division Algorithm to find the HCF of 726 and 275.
14. Prove that $\sqrt{7}$ is an irrational number.
15. Prove that: $(\operatorname{cosec} A-\sin A)(\sec A-\cos A)=\frac{1}{\tan A+\cot A}$
(OR)
Prove that: $(1+\cot A-\operatorname{cosec} A)(1+\tan A+\sec A)=2$.
16. Solve the following system of equations for x and $\mathrm{y}: \frac{5}{x-1}+\frac{1}{y-2}=2, \frac{6}{x-1}-\frac{3}{y-2}=1$
17. Show that $\triangle A B C$, where $A(-2,0), B(2,0), C(0,2)$ and $\triangle P Q R$ where $P(-4,0), Q(4,0), R(0,4)$ are similar triangles.

The area of a triangle is 5 sq. units. Two of its vertices are $(2,1)$ and $(3,-2)$. If the third vertex is $\left(\frac{7}{2}, y\right)$, find the value(s) of $y$.
18. Two different dice are thrown together. Find the probability that the numbers obtained (i) have a sum less than 5 (ii) have a product less than 6 (iii) is a doublet of even numbers.
19. A top is shaped like a cone surmounted by a hemisphere. The entire top is 7 cm in height and the diameter of the top is 6 cm . If a child wants to colour the top, find the area he has to colour. (Use $=\frac{22}{7}$ ).
20. Two tangents TP and TQ are drawn to a circle with centre O from an external point T . Prove that $\angle \mathrm{PTQ}=2$ $\angle O P Q$.

## (OR)

In the given figure, AC and AD are tangents to a circle with centre O , at C and D respectively. If $\angle \mathrm{BCD}=44^{\circ}$, then find $\angle \mathrm{CAD}, \angle \mathrm{CBD}$ and $\angle A C D$

21. In a hospital used water is collected in a cylindrical tank of diameter 4 m and height 5 m . After recycling, this water is used to irrigate a park of hospital whose length is 25 m and breadth is 20 m . If tank is filled completely then what will be the height of standing water used for irrigating the park.
(OR)
The radii of internal and external surfaces of a hollow spherical shell are 3 cm and 5 cm respectively. It is melted and recast into a solid cylinder of diameter 14 cm . Find the height of the cylinder
22. Find the ratio in which the $y$-axis divides the line segment joining the points $(5,-6)$ and $(-1,-4)$. Also find the point of intersection

## SECTION D

(Questions 23 to 30 carry 4 marks each)
23. On dividing the polynomial $3 x^{3}+4 x^{2}+5 x-13$ by a polynomial $g(x)$, the quotient and the remainder were $(3 x+10)$ and $(16 x-43)$ respectively. Find $g(x)$.
24. Prove that the lengths of tangents drawn from an external point to a circle are equal.
25. From the top of a 60 m high building, the angles of depression of the top and the bottom of a tower are observed to be $30^{\circ}$ and $60^{\circ}$ respectively. Find the height of the tower.

The angle of elevation of the top of a tower from certain point is $30^{\circ}$. If the observer moves 20 m towards the tower, the angle of elevation of the top increased by $15^{\circ}$. Find the height of the tower.
26. A boat goes 30 km upstream and 44 km downstream in 10 hours. In 13 hours, it can go 40 km upstream and 55 km downstream. Determine the speed of the stream and that of the boat in still water.
(OR)
2 men and 7 women can do a piece of work in 4 days. It is done by 4 men and 4 women in 3 days. How long would it take for one man or one woman to do it?
27. Construct a $\triangle A B C$ in which $\mathrm{BC}=6.5 \mathrm{~cm}, \mathrm{AB}=4.5 \mathrm{cmand} \angle A C B=60^{\circ}$. Construct another triangle similar to $\triangle A B C$ such that each side of new triangle is $\frac{4}{5}$ of the corresponding sides of $\triangle A B C$
28. A drinking glass is in the shape of a frustum of a cone of height 14 cm . The diameters of its two circular ends are 16 cm and 12 cm . Find the capacity and surface area of the glass. ( $\mathrm{Use} \sqrt{2}=1.4, \pi=\frac{22}{7}$ )
29. Draw 'more than Ogive' for the following distribution and hence find its median.

| Class | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 8 | 12 | 24 | 6 | 10 | 15 | 25 |

30. If the mean of the following frequency distribution is 65.6 , find the missing frequencies:

| Class | $10-30$ | $30-50$ | $50-70$ | $70-90$ | $90-110$ | $110-130$ | Total |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 5 | 8 | $\mathrm{f}_{1}$ | 20 | $\mathrm{f}_{2}$ | 2 | 50 |

(OR)
The median of the following data is 32.5 . Find the values of $x$ and $y$, if the total frequency is 40 .

| Class | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ | $50-60$ | $60-70$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | x | 5 | 9 | 12 | y | 3 | 2 |

## End of the Question Paper

